

# **Causal mediation analysis of observational, population-based cancer survival data**

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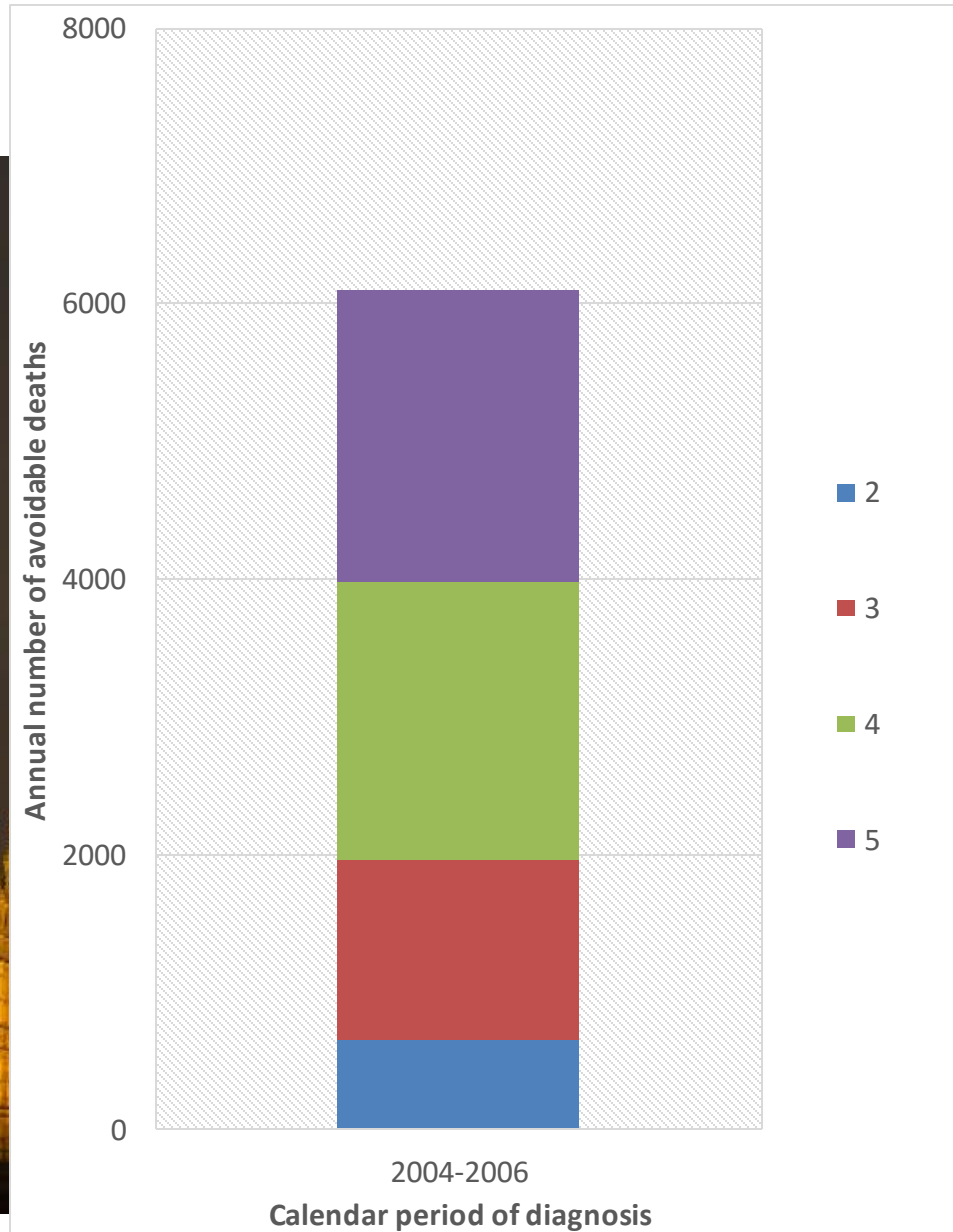


# Outline

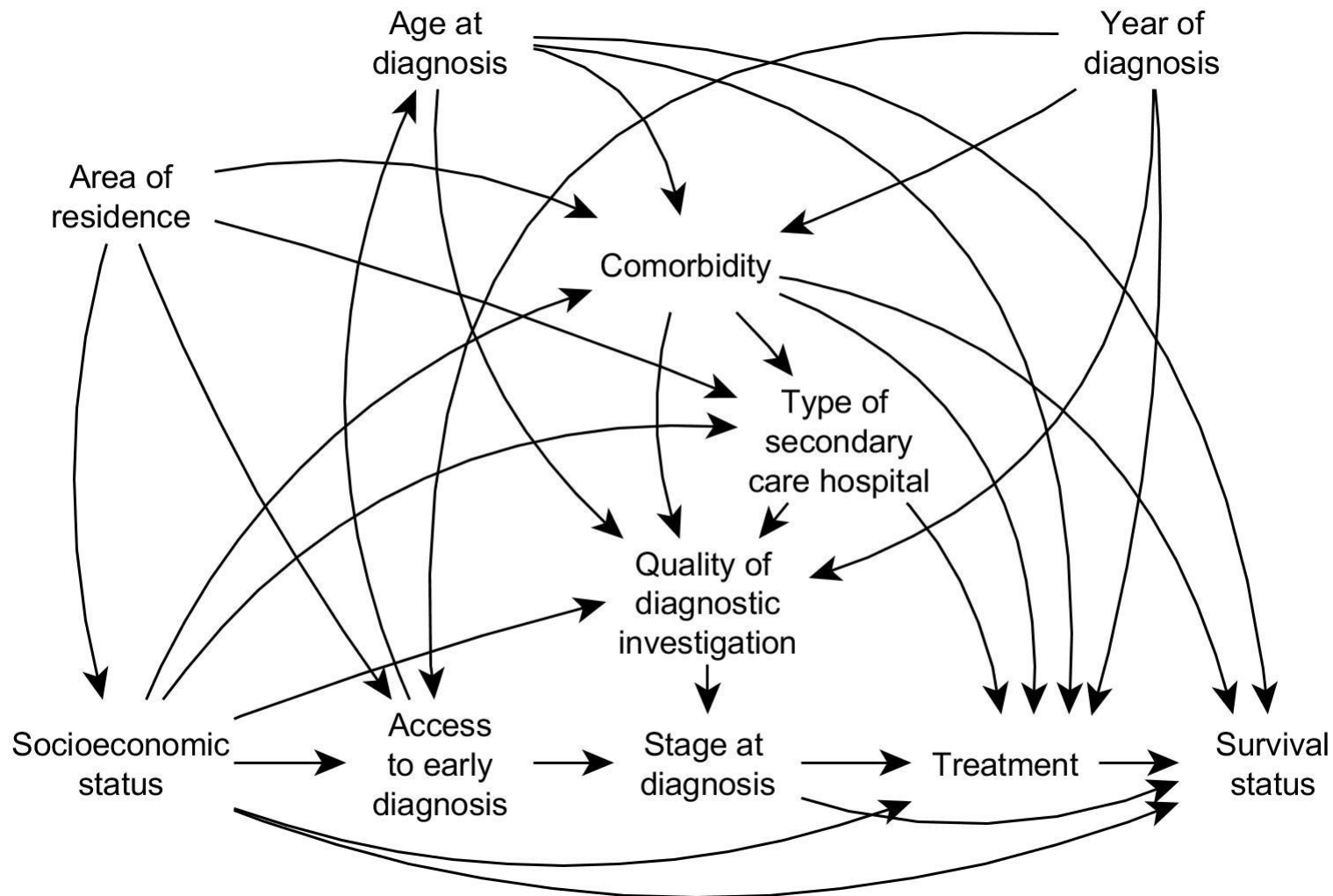
- Main questions
- Challenges with conventional approaches – results from the past
- An example of applying mediation to cancer survival data
- Problems and discussions
  - Misclassification of mediators
    - Treatment missing for more affluent – sensitivity analysis
    - Under-staged deprived patients – sensitivity analysis
  - Biases for mediation analyses
  - Controlled and natural effects
  - Conceptual frameworks – Suggestions?
    - Including issue of diagnosed stage *versus* real stage



# Inequalities in cancer survival



# Explaining inequalities



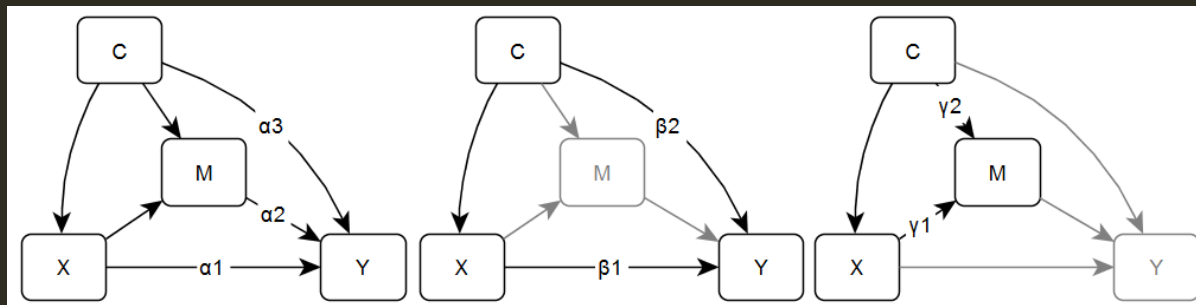
# Challenges in the past

- **More deprived patients:**
  - More comorbidity
  - More advanced cancer at diagnosis (colon, rectum, breast)
  - More often diagnosed during emergency admission
  - More often treated in non-specialised hospital and by non-specialised surgeon
  - Received more often sub-optimal and delayed treatment (colon, rectum)
- **Past conventional analysis (colon, rectum, breast)**
  - No excess mortality hazard for deprivation among those treated within one month since diagnosis
  - Adjusting for comorbidity did not modify the excess mortality hazard for deprivation
  - Adjusting for stage reduced the excess mortality hazard for deprivation by less than a third
  - Limited stage and treatment data and conventional analytic approaches did not enable identification of mechanisms underlying deprivation gap in survival



NB: explain DAG

# TRADITIONAL MEDIATION ANALYSIS

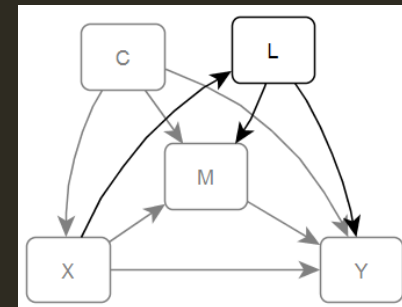


Difference method (Baron and Kenny, 1986)

Product method (Wright, 1921)

## Problems

- Definition of effects model-dependent
- Inflexible: interaction & non-linearity
- Intermediate confounder



# COUNTERFACTUAL APPROACHES

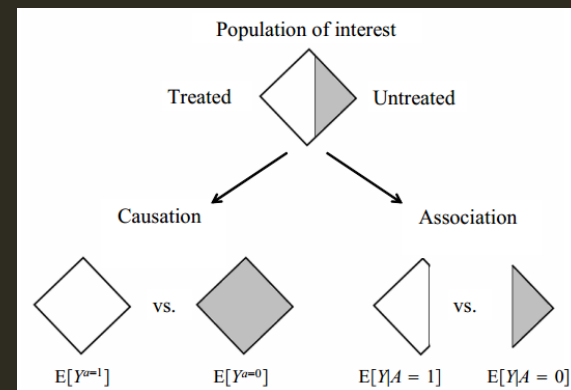
	A	Y
Rhea	0	0
Kronos	0	1
Demeter	0	0
Hades	0	0
Hestia	1	0
Poseidon	1	0
Hera	1	0
Zeus	1	1
Artemis	0	1
Apollo	0	1
Leto	0	0
Ares	1	1
Athena	1	1
Hephaestus	1	1
Aphrodite	1	1
Cyclope	1	1
Persephone	1	1
Hermes	1	0
Hebe	1	0
Dionysus	1	0

Observed

	$Y^{a=0}$	$Y^{a=1}$
Rhea	0	1
Kronos	1	0
Demeter	0	0
Hades	0	0
Hestia	0	0
Poseidon	1	0
Hera	0	0
Zeus	0	1
Artemis	1	1
Apollo	1	0
Leto	0	1
Ares	1	1
Athena	1	1
Hephaestus	0	1
Aphrodite	0	1
Cyclope	0	1
Persephone	1	1
Hermes	1	0
Hebe	1	0
Dionysus	1	0

Counterfactual worlds

- Notations:  $Y(x)$ ,  $Y(x,m)$ ,  $Y(x,M(x))$



From: <http://www.hsph.harvard.edu/miguel-hernan/causal-inference-book/>

# CAUSAL APPROACHES ALLOWS MODEL-FREE DEFINITION OF EFFECTS...

Total causal effect

- $TCE = E(Y[1, M(1)]) - E(Y[0, M(0)])$

Natural direct effect

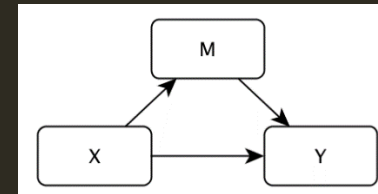
- $NDE(0) = E(Y[1, M(0)]) - E(Y[0, M(0)])$

Natural indirect effect

- $NIE(1) = E(Y[1, M(1)]) - E(Y[1, M(0)])$

Controlled direct effect

- $CDE(m) = E(Y[1, m]) - E(Y[0, m])$

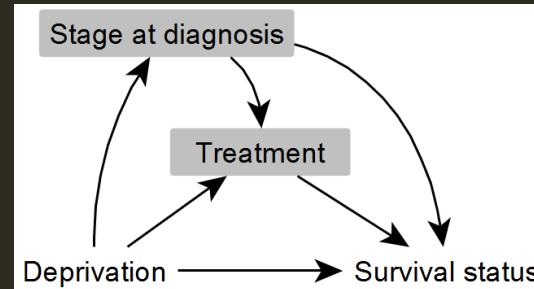


## Assumptions for identification

- 1: no unmeasured confoundings
- 2: no exposure induced M/Y confounder (L)



# BUT WE HAVE L...



- Important mediator-outcome confounders affected by exposure
- Likely presence of many interactions
- Binary outcome

One of the solutions proposed in VanderWeele, Vansteelandt and Robins (Epidemiology 2014)

## Interventional effect

- Randomized interventional analogues of natural direct and indirect effects
- Estimated with an extension of Robins' g-computation formula implemented using Monte Carlo simulation
- Similar definitions to NIE and NDE

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# How much of the socioeconomic differences in breast cancer patient survival can be explained by stage at diagnosis and treatment?

Application of causal mediation analysis to routine data

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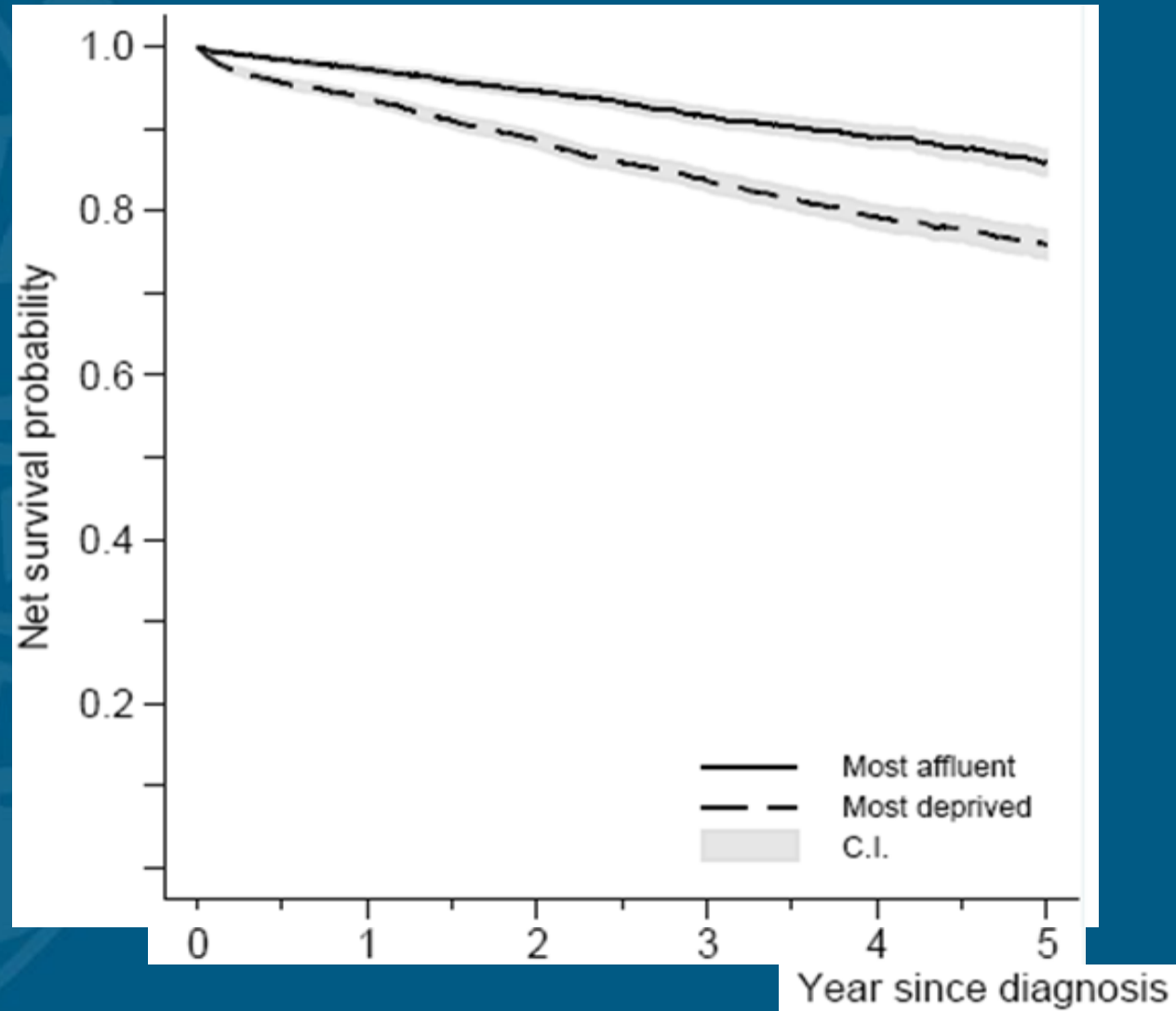


# Introducing breast cancer

- Most common cancer in the UK
- Screening (50-70)
- Treatment with strict guidelines
- Northern and Yorkshire Cancer Registry, population-based, covering 12% of the English population
- Women with malignant breast cancers (N=36,793)
  - Diagnosed during the period 2000–2007
  - Followed up until 31 December 2007



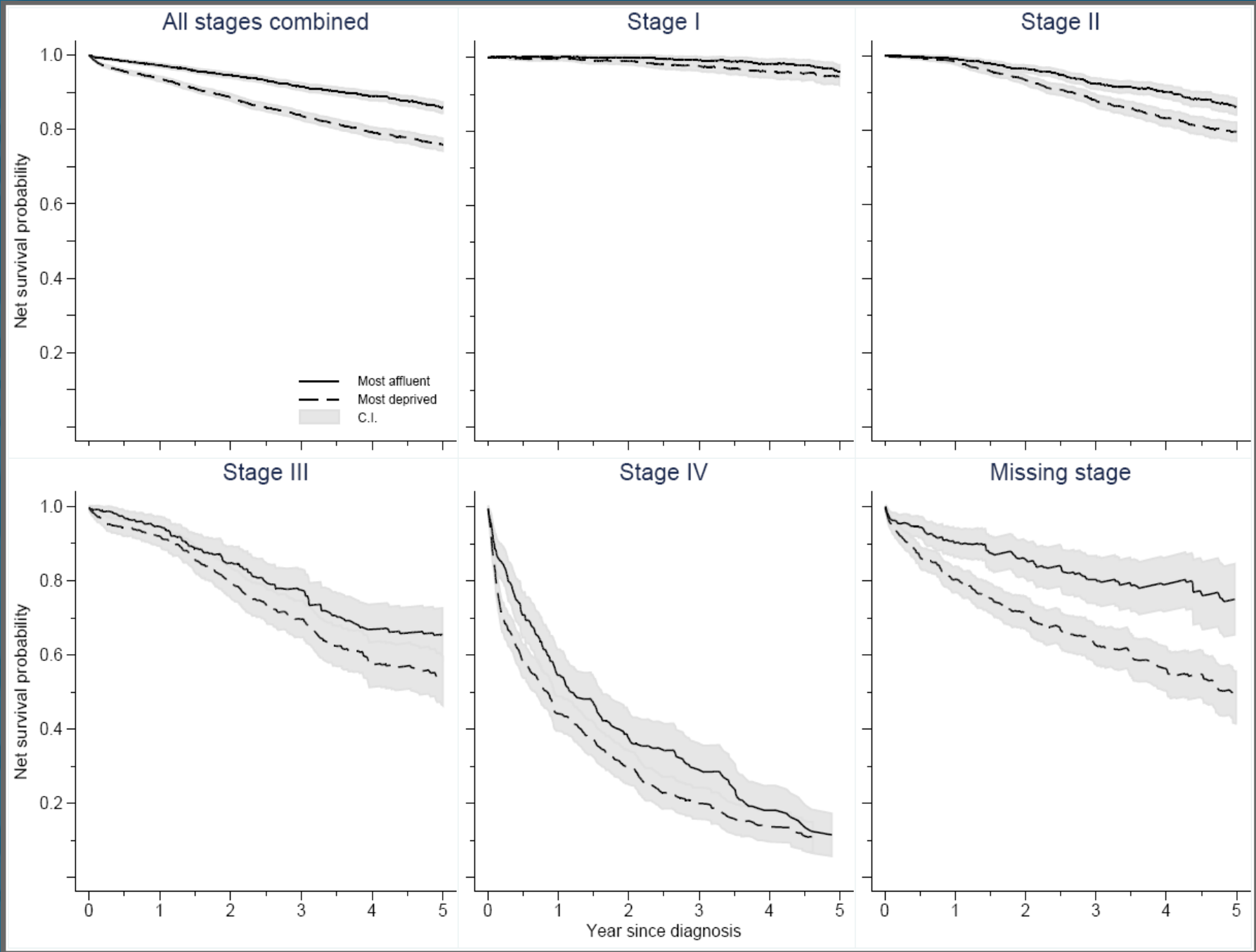
# Large deprivation gap in survival from breast cancer...



# Possible explanations

- Differential stage at diagnosis?
- Differential treatment?

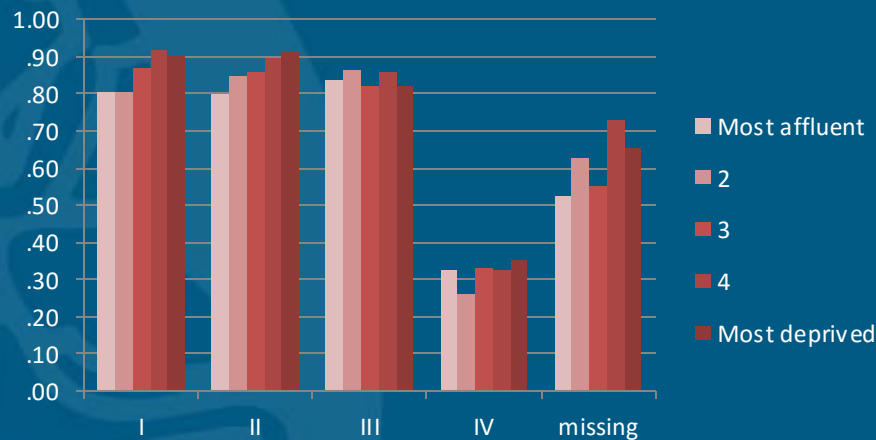




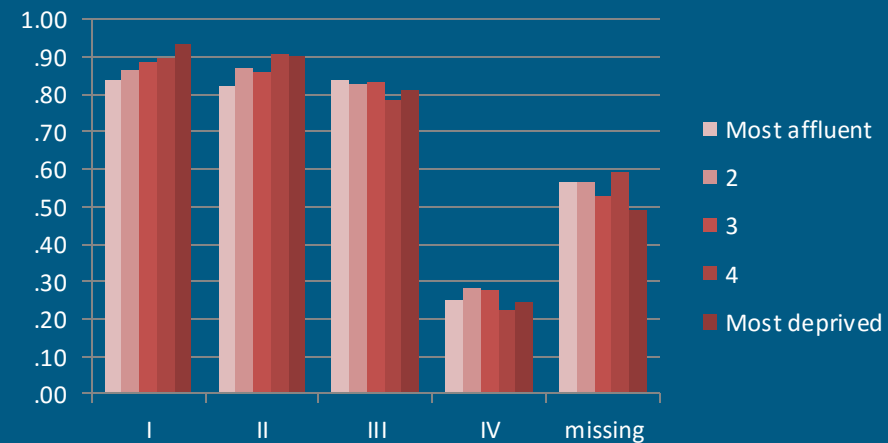
# Differential treatment?

## – probability of getting major surgery

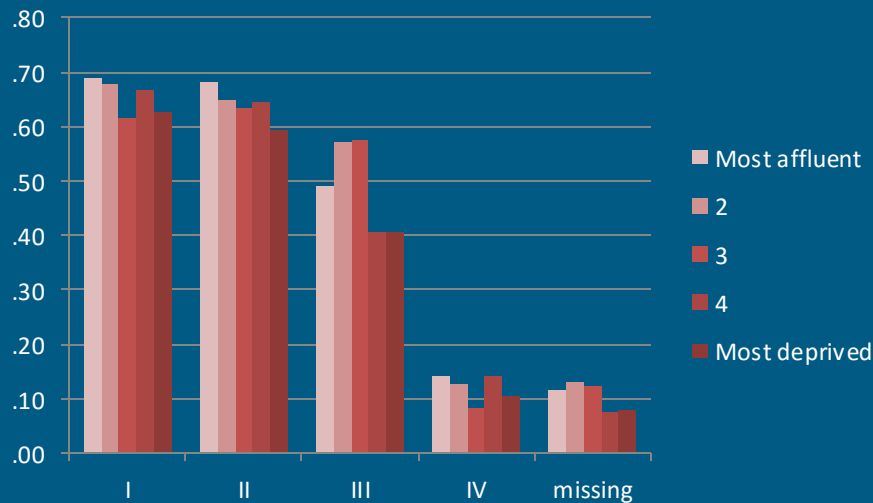
15-49 pre-screening



50-69 screening

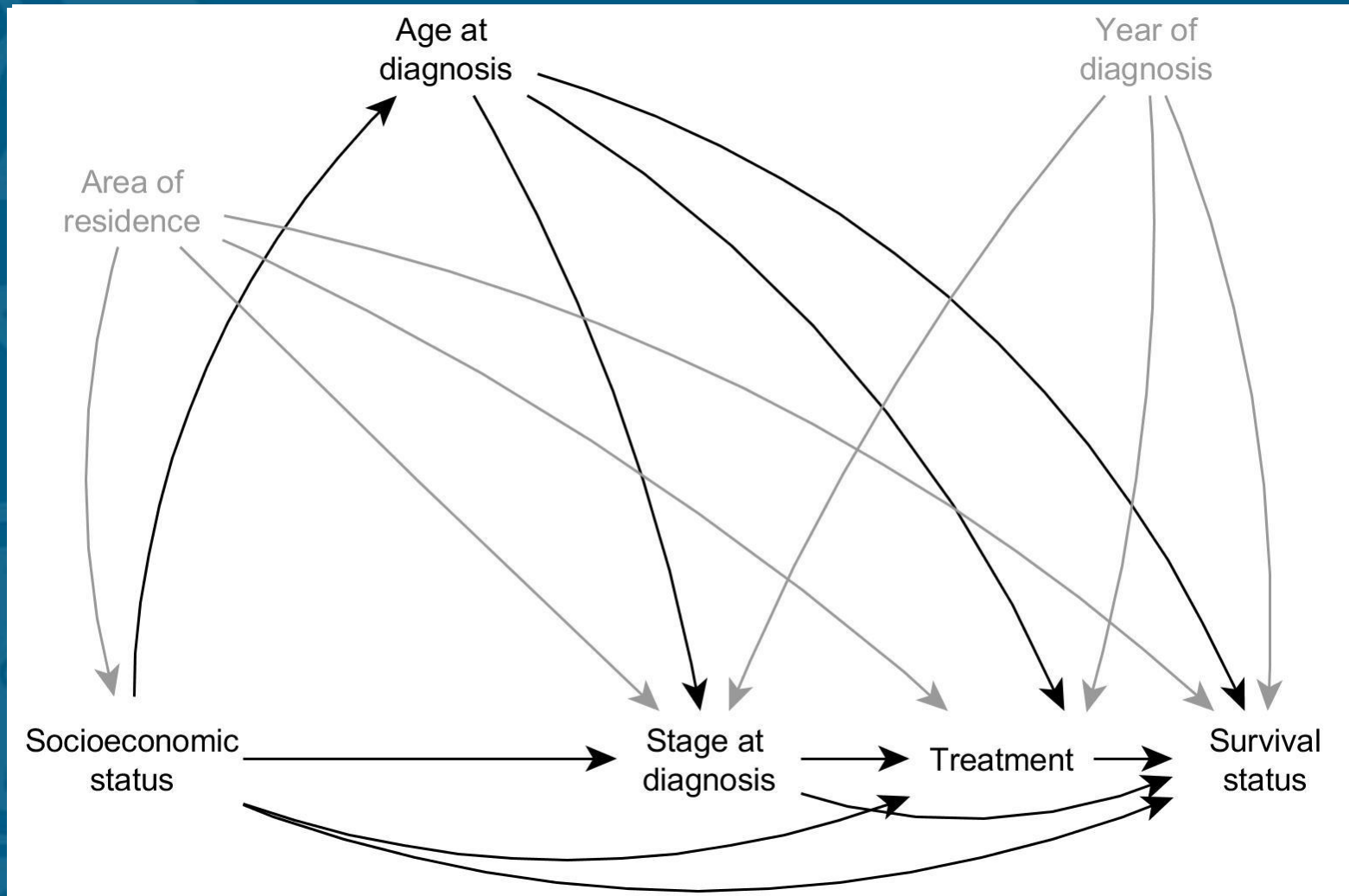


70+  
post-screening

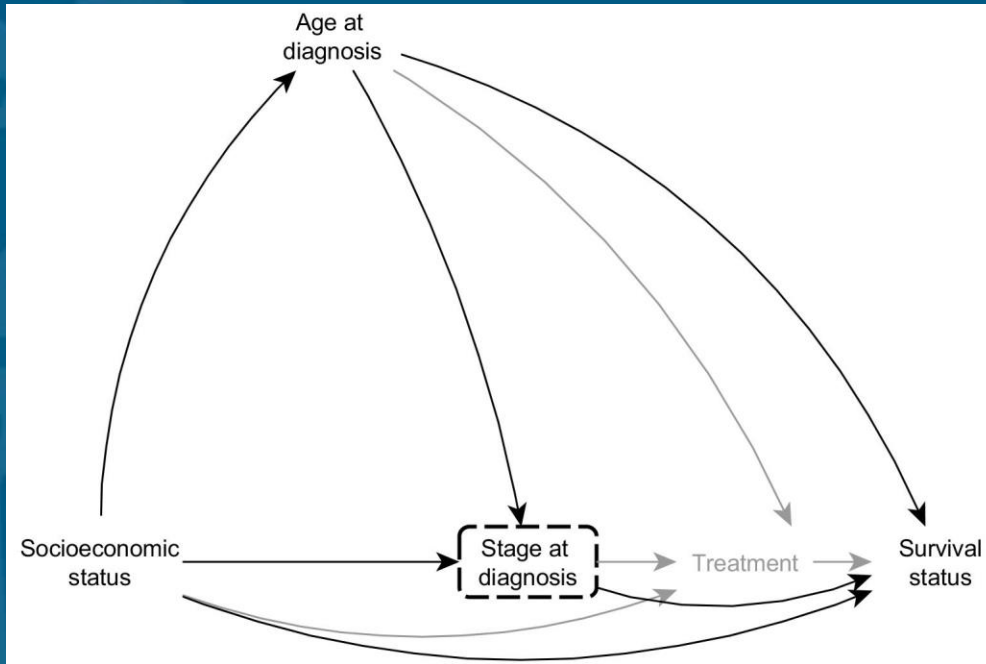




# Linking to the conceptual diagram...



# If we look at stage



We can **decompose** the total effect (TCE) of socioeconomic status (deprivation) on mortality into...

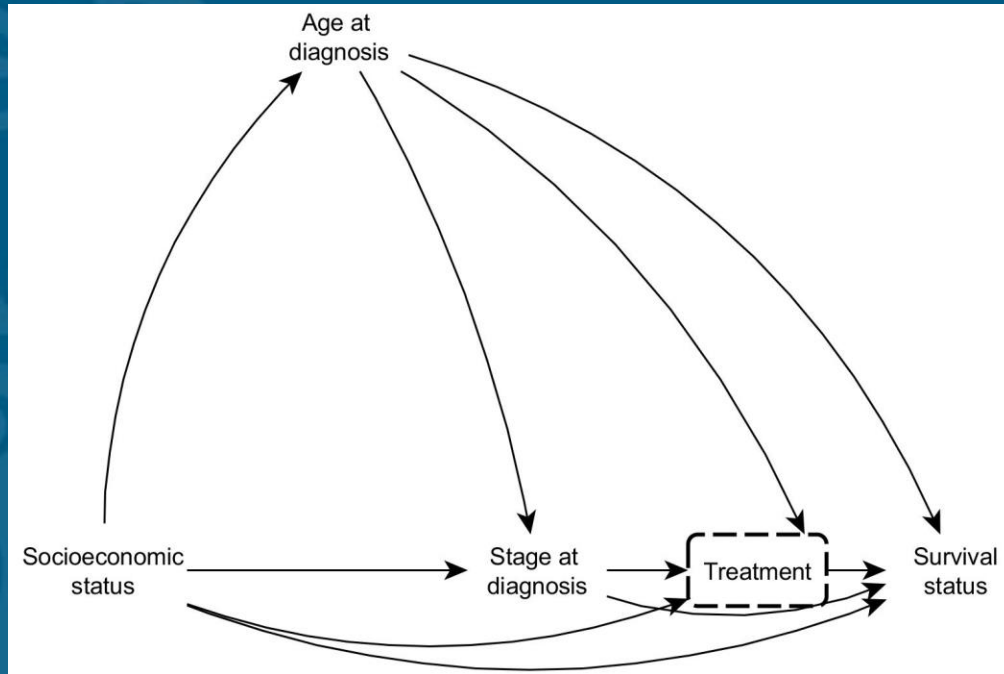
- Those mediated by stage (The indirect effect, NIE)
- Those not mediated by stage (The direct effect, NDE)

$$\text{TCE} = \log(\text{odds}(Y(\text{Dep}=\text{most}, \text{Stage}(\text{Dep}=\text{most})))) - \log(\text{odds}(Y(\text{Dep}=\text{least}, \text{Stage}(\text{Dep}=\text{least}))))$$

$$\text{NIE} = \log(\text{odds}(Y(\text{Dep}=\text{most}, \text{Stage}(\text{Dep}=\text{most})))) - \log(\text{odds}(Y(\text{Dep}=\text{most}, \text{Stage}(\text{Dep}=\text{least}))))$$

$$\text{NDE} = \log(\text{odds}(Y(\text{Dep}=\text{most}, \text{Stage}(\text{Dep}=\text{least})))) - \log(\text{odds}(Y(\text{Dep}=\text{least}, \text{Stage}(\text{Dep}=\text{least}))))$$

# If we look at treatment



We can **decompose** the total effect (TCE) of deprivation on mortality into...

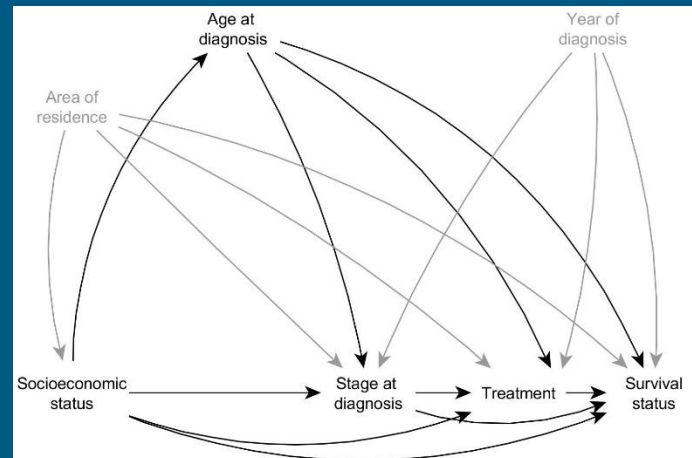
- Those mediated by treatment (The indirect effect, NIE)
- Those not mediated by treatment (The direct effect, NDE)

$$\text{TCE} = \log(\text{odds}(Y(\text{Dep}=\text{most}, \text{Treat}(\text{Dep}=\text{most})))) - \log(\text{odds}(Y(\text{Dep}=\text{least}, \text{Treat}(\text{Dep}=\text{least}))))$$

$$\text{NIE} = \log(\text{odds}(Y(\text{Dep}=\text{most}, \text{Treat}(\text{Dep}=\text{most})))) - \log(\text{odds}(Y(\text{Dep}=\text{most}, \text{Treat}(\text{Dep}=\text{least}))))$$

$$\text{NDE} = \log(\text{odds}(Y(\text{Dep}=\text{most}, \text{Treat}(\text{Dep}=\text{least})))) - \log(\text{odds}(Y(\text{Dep}=\text{least}, \text{Treat}(\text{Dep}=\text{least}))))$$

# G-formula results

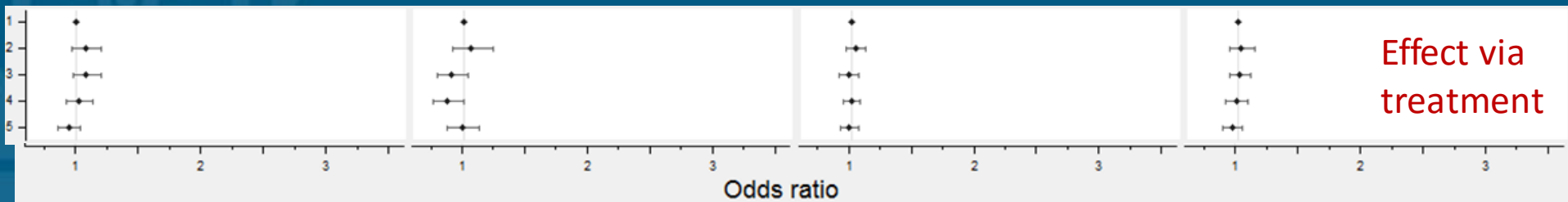
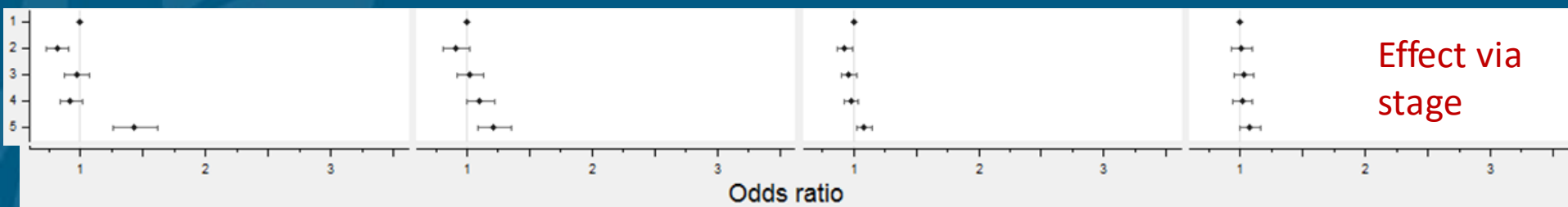
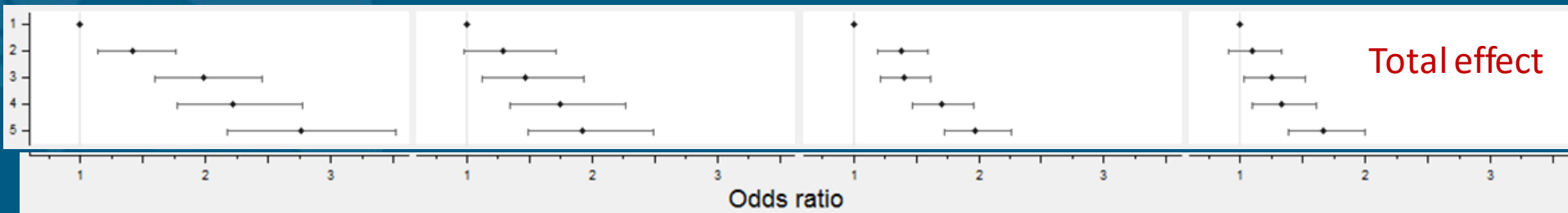


6 months

12 months

3 years

5 years



# Preliminary conclusions

- Breast cancer survival differed between the most deprived and most affluent patients
- Effect of deprivation on mortality:
  - Large total effect **FOR ALL DEPRIVATION CATEGORIES:**
    - Increasing with deprivation
    - Decreasing with time since diagnosis
  - Mediated via stage **ONLY FOR MOST DEPRIVED CATEGORY:**
    - One third of at six months
    - One tenth at three/five years since diagnosis
  - Mediated via treatment:
    - None



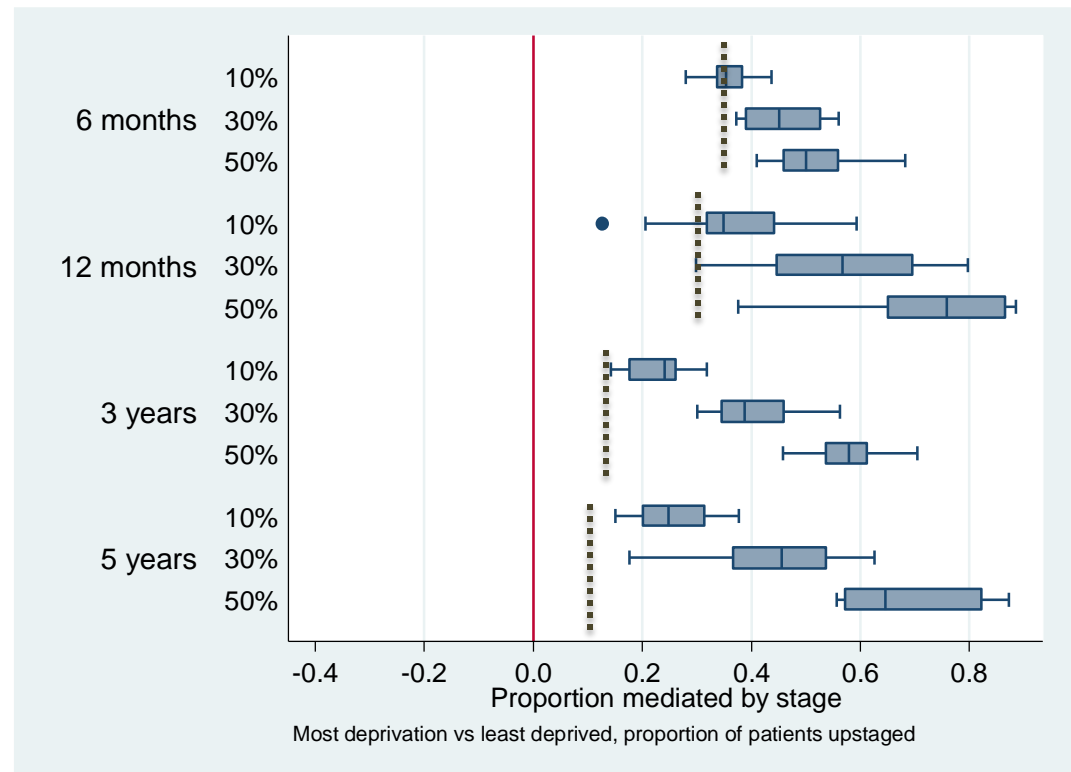
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# Misclassification of stage

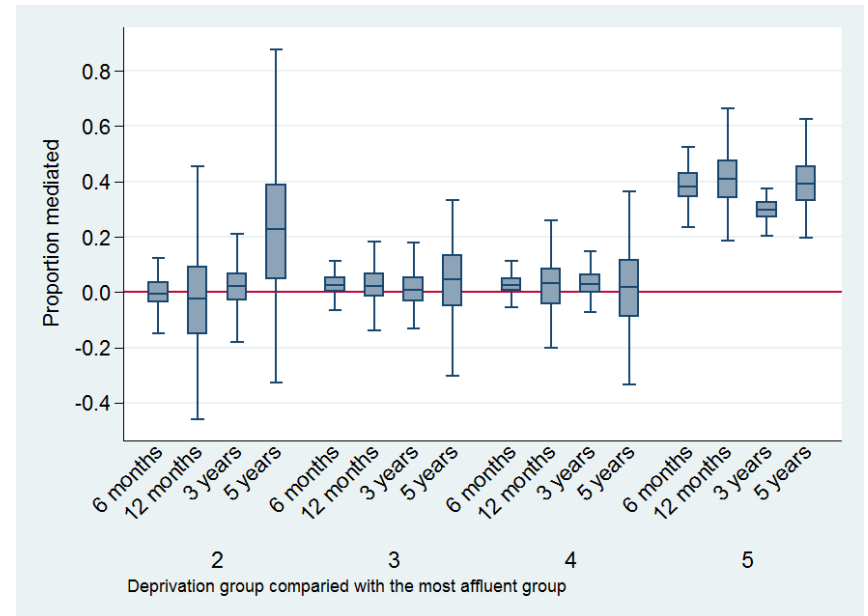
- More deprived patients may be under-staged?
- Randomly “up-staging” 10%, 30% and 50% of most deprived patients...
- 10% up-staging did not change results much
- After 30%-50% upstaging, stage would mediate more than half of the survival differences
- Longer-term survival is more affected ...





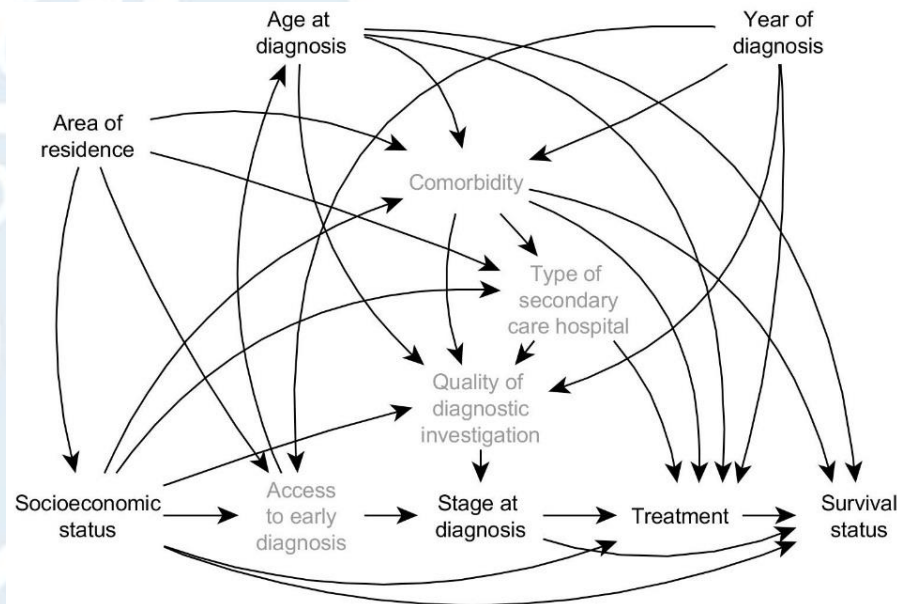
# Misclassification of treatment

- One report showed that 4% of surgical treatment for breast cancer were made in private hospital
- Sensitivity analysis:
  - Assumption: all missing surgery is among most affluent patients
  - Randomly adding “major surgery” to 4% of women, all from the most affluent category
- Now treatment mediates survival differences for the most deprived!



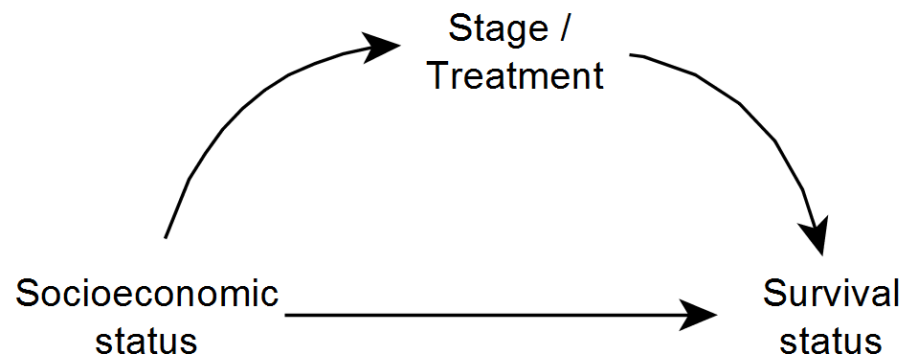


# Biases for mediation analysis



- Unmeasured or poorly measured confounders, e.g. between mediator and outcome?
- Presence of confounder(s) between mediator and outcome affected by exposure?

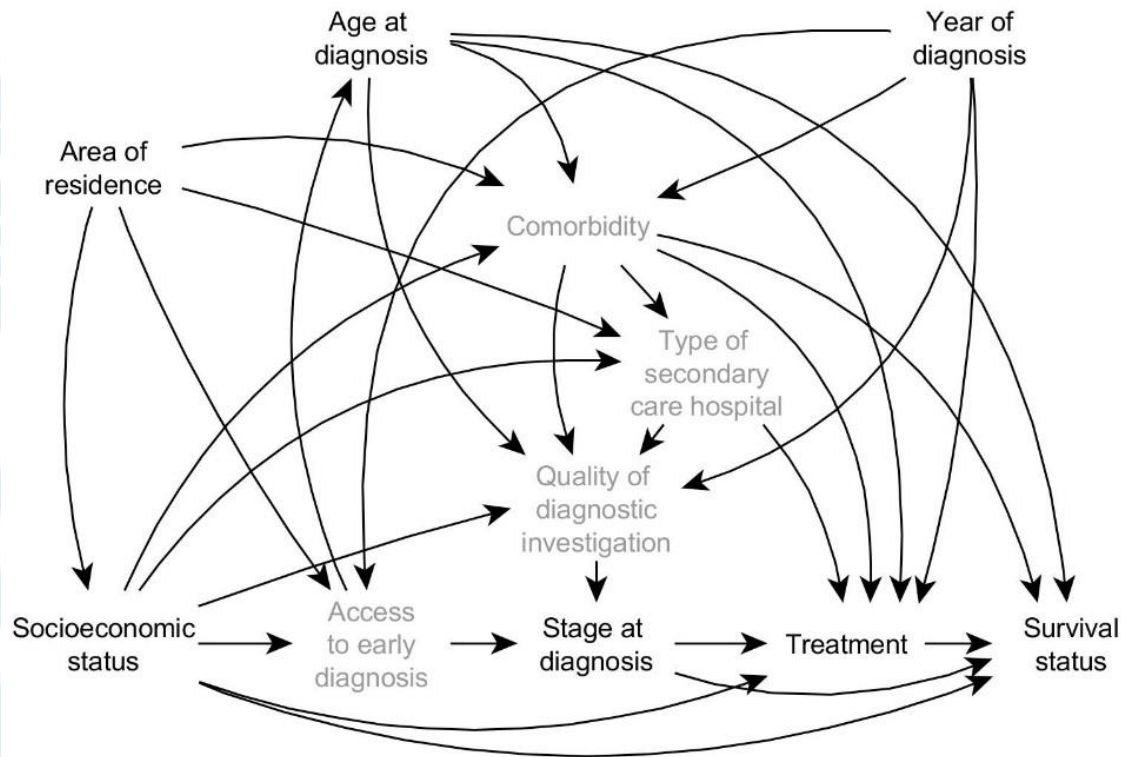
# Controlled vs natural effects



- Natural direct effect
  - What effect would SES have on survival status if the more deprived patients had the stage/treatment distribution of the most affluent patients?
  - It measures delays in diagnosis (stage) or inequities in management (treatment)
- Controlled direct effect
  - What effect does SES have on survival status if we intervened on everyone's diagnosed stage/treatment and set it to a particular level?
  - More sensible to estimate CDE for compliance to treatment guideline?
    - Classify treatment as *compliant to guideline* (Yes/No) according to detailed patient and tumour characteristics
    - Mediator = compliance to guideline



# Conceptual framework



- Among more deprived patients:
  - Sub-optimal diagnostic investigation
  - Wider discrepancy between true and observed stage
- How to account for this stage misclassification?

# Summary

- First application of the causal mediation tool in study of cancer registry data
- Population-based data
- Drawbacks
  - Data quality and detail
  - Unmeasured confounder, e.g. comorbidity
- Useful for answering questions related to causality
  - Resource allocation



# References

- Woods L. M., Rachet B., Coleman M. P. 2005 Origins of socio-economic inequalities in cancer survival: a review. *Ann Oncol* 17(1):5-19
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- VanderWeele TJ, Vansteelandt S, Robins JM. Effect Decomposition in the Presence of an Exposure-Induced Mediator-Outcome Confounder. *Epidemiology*. 2014;25(2):300-6.

